

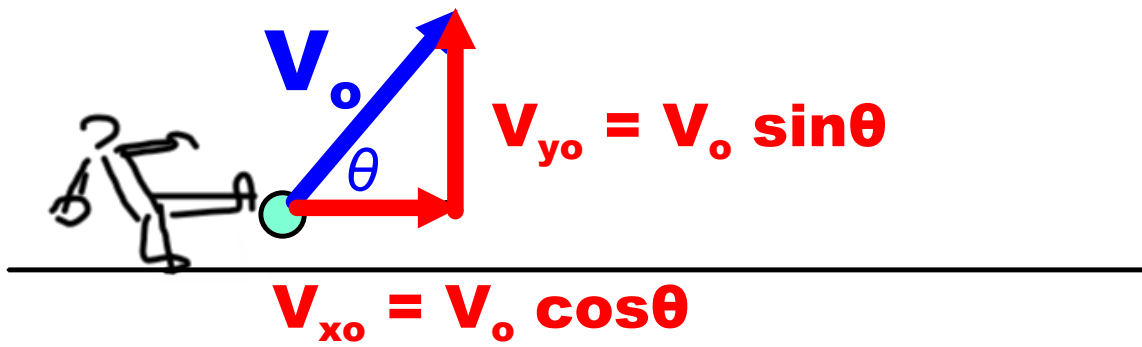
**Before starting these problems,
there is an initial step.**



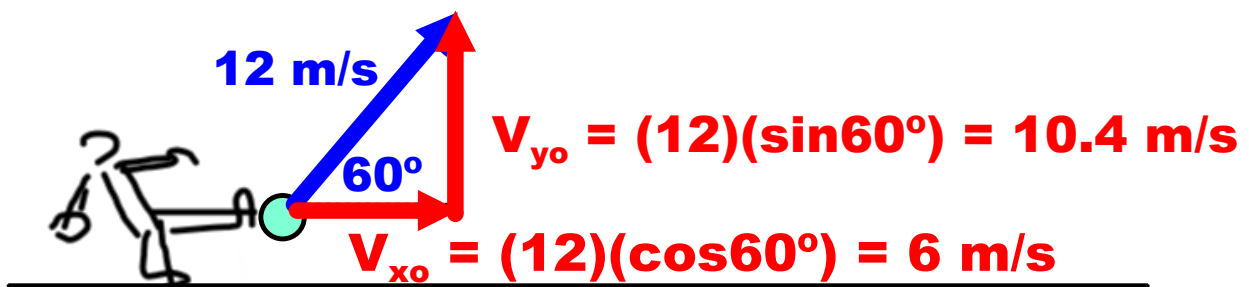
The initial velocity has to be broken into components.



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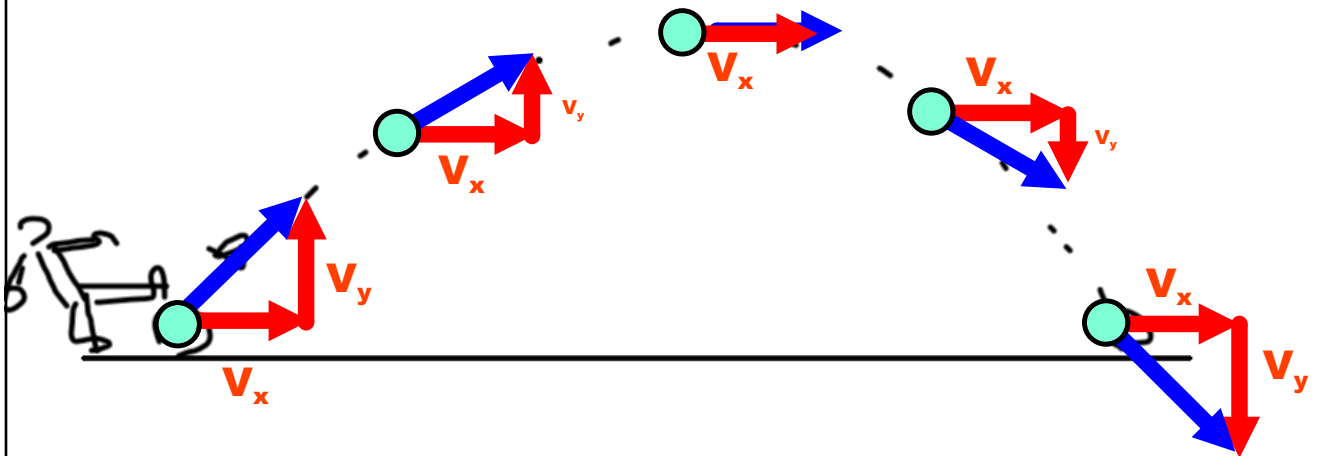


Once you do that, you never use the 12 m/s again!

Things we know:

V_x is constant the whole way.

V_y slows down on the way up, speeds back up on the way down.



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V_x is constant the whole way.

V_y slows down on the way up, speeds back up on the way down.

$V_y = 0$ at the top



plugging in $V_y = 0$

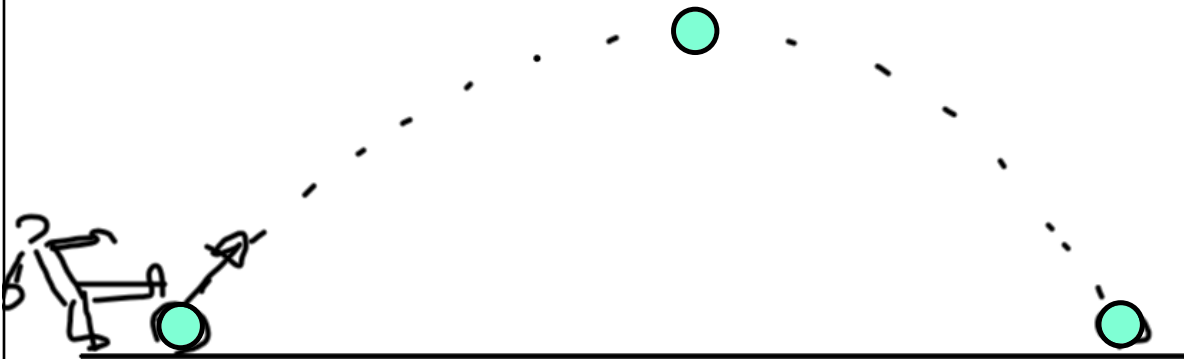
$$V_y = V_{yi} + a_y t$$

$$V_y^2 = V_{yo}^2 + 2a_y \Delta y$$

**Can get you time
to top or Δy_{\max}**

$(a_y \text{ is always } -10\text{m/s}^2)$

Things we know:



$\Delta y = 0$ when it gets
back down.

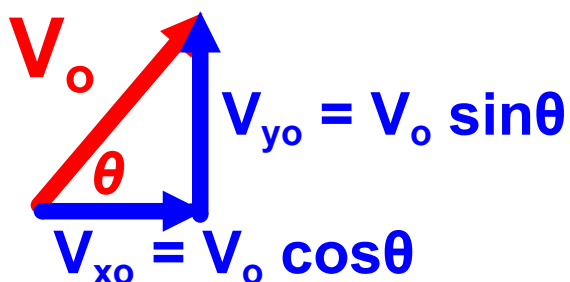
plugging in $\Delta y = 0$

$$\Delta y = V_{yo}t + \frac{1}{2}a_y t^2$$

Can get you the
time to go all
the way



$(a_y \text{ is always } -10\text{m/s}^2)$

angled launches

$$\Delta x = V_{xo}t$$

Use to get how far in the x (range).

$$\Delta y = V_{yo}t + 1/2a_yt^2$$

$$V_y = V_{yo} + a_yt$$

$$V_y^2 = V_{yo}^2 + 2a_y\Delta y$$

$$(a_y \text{ is } -10\text{m/s}^2)$$

Set $V_y = 0$ to get the time to the top and double it.

Set $V_y = 0$ to get Δy_{max} (max ht at the top)



2. The baseball is hit from and caught at the same height.

- Resolve the initial velocity into components.
- How long was the ball in flight?
- What horizontal distance did the ball travel?
- How high above the start height did the ball get?



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$$(a) V_{xo} = (50 \text{ m/s})\cos 25^\circ = 45.3 \text{ m/s}$$

$$V_{yo} = (50 \text{ m/s})\sin 25^\circ = 21.1 \text{ m/s}$$

$$(b) V_y = V_{yo} + at$$

($V_y = 0$ at the top)

$$0 = (21.1) + (-10)t$$

$$0 = 21.1 - 10t$$

$$10t = 21.1$$

$$t = 2.11 \text{ s}$$

double it!

$$t = 4.22 \text{ s}$$

$$(c) \Delta x = V_{xo}t$$

(find Δx at the total time)

$$\Delta x = (45.3)(4.2)$$

$$\Delta x = 190.3 \text{ m}$$

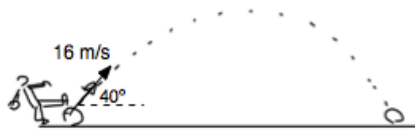
$$(d) V_y^2 = V_{yo}^2 + 2a_y\Delta y$$

($V_y = 0$ at the top when it hits Δy_{\max})

$$0^2 = 21.1^2 + 2(-10)\Delta y_{\max}$$

$$0 = 446.5 - 20\Delta y_{\max}$$

$$22.3 \text{ m} = \Delta y_{\max}$$



The soccer ball is kicked from and lands at the same height.

- Resolve the initial velocity into components.
- How long was the ball in flight?
- What horizontal distance did the ball travel?
- How high above the start height did the ball get?

$$a) \begin{aligned} v_{xo} &= v_o \cos \theta = (16) \cos 40^\circ = 12.3 \text{ m/s} \\ v_{yo} &= v_o \sin \theta = (16) \sin 40^\circ = 10.3 \text{ m/s} \end{aligned}$$

$$b) v_y = v_{yo} + a_y t$$

$$0 = 10.3 + (-10)t$$

$$10t = 10.3$$

$$t = 1.03 \text{ double it!} \rightarrow 2.06 \text{ s}$$

$$c) \begin{aligned} \Delta x &= v_{xo} t \\ &= (12.3)(2.06) \\ &= 25.3 \text{ m} \end{aligned}$$

$$d) v_y^2 = v_{yo}^2 + 2a_y \Delta y$$

$$0 = 10.3^2 + 2(-10)\Delta y$$

$$0 = 106.1 - 20\Delta y$$

$$20\Delta y = 106.1$$

$$\Delta y = 5.3 \text{ m}$$



The soccer ball is kicked from and lands at the same height.

- a) Resolve the initial velocity into components.
- b) How long was the ball in flight?
- c) What horizontal distance did the ball travel?
- d) How high above the start height did the ball get?

Try it!

See if you can get these answers:

(a) $V_{x0} = 12.3 \text{ m/s}$

$V_{y0} = 10.3 \text{ m/s}$

(b) $t = 2.06 \text{ s}$

(c) $\Delta x = 25.3 \text{ m}$

(d) $\Delta y_{\text{max}} = 5.3 \text{ m}$



The baseball is hit from and caught at the same height. **additional**

- Resolve the initial velocity into components.
- How long was the ball in flight?
- What horizontal distance did the ball travel?
- How high above the start height did the ball get?



The baseball is hit from and caught at the same height.

additional

- Resolve the initial velocity into components.
- How long was the ball in flight?
- What horizontal distance did the ball travel?
- How high above the start height did the ball get?

$$(a) V_{x0} = (40 \text{ m/s})\cos 30^\circ = 34.6 \text{ m/s}$$

$$V_{y0} = (40 \text{ m/s})\sin 30^\circ = 20 \text{ m/s}$$

$$(b) \Delta y = V_{y0}t + \frac{1}{2}a_y t^2$$

(total time is when $\Delta y = 0$)

$$0 = (20)t + \frac{1}{2}(-10)t^2$$

$$0 = 20t - 5t^2$$

$$0 = t(20 - 5t)$$

$$\text{either } t = 0 \text{ or } (20 - 5t) = 0$$

$$\text{so } t = 0 \text{ or } t = 20/5 = 4 \text{ sec.}$$

at the start

at the end

$$(c) \Delta x = V_{x0}t$$

(find Δx at the total time)

$$\Delta x = (34.6)(4)$$

$$\Delta x = 139 \text{ m}$$

$$(d) V_y^2 = V_{y0}^2 + 2a_y \Delta y$$

(set $V_y = 0$ to get Δy_{\max})

$$0^2 = 20^2 + 2(-10)\Delta y_{\max}$$

$$0 = 400 - 20\Delta y_{\max}$$

$$20 \text{ m} = \Delta y_{\max}$$



The soccer ball is kicked from and lands at the same height.

additional

- a) Resolve the initial velocity into components.
- b) How long was the ball in flight?
- c) What horizontal distance did the ball travel?
- d) How high above the start height did the ball get?

Try it!

See if you can get these answers:

a) $v_{x0} = 11.5 \text{ m/s}$ c) 37.7 m

$v_{y0} = 16.4 \text{ m/s}$

b) 3.27 s

d) 13.4 m